

Unifying inflation and dark matter with neutrino masses

Rouzbah Allahverdi^{1,2}, Bhaskar Dutta³, and Anupam Mazumdar^{4,5}

¹ *Perimeter Institute for Theoretical Physics, Waterloo, ON, N2L 2Y5, Canada*

² *Department of Physics and Astronomy, University of New Mexico, Albuquerque, NM 87131, USA*

³ *Department of Physics, Texas A&M University, College Station, TX 77843-4242, USA*

⁴ *NORDITA & Niels Bohr Institute, Blegdamsvej-17, Copenhagen-2100, Denmark*

⁵ *Physics Department, Lancaster University, LA1 4YB, UK*

We propose a simple model where a *gauge invariant inflaton* is responsible for cosmic inflation and generates the seed for structure formation, while its relic *thermal* abundance explains the missing matter of the universe in the form of cold dark matter. The inflaton self-coupling also explains the observed neutrino masses. All the virtues can be attained in a minimal extension of the Standard Model gauge group around the TeV scale. We can also unveil these properties of an inflaton in forthcoming space and ground based experiments.

There are three important puzzles, the origin of inflation, the origin of cold dark matter, and the origin of neutrino masses, which require explanation in any extension of the electroweak standard model (SM). The aim of this paper is to bind the three issues together and explain all of them in a single set up. Inflation is driven by a scalar field known as the *inflaton*, for a review see [1]. In this paper we shall illustrate an inflaton part of which directly decays into the SM baryons, its *thermal* relic abundance accounts for the missing matter in the universe, commonly known as cold dark matter, and also explains the observed neutrino masses.

The inflaton potential explains the flatness of the universe and also the observed anisotropy in the cosmic microwave background (CMB) temperature, i.e. $\delta_H \sim 1.91 \times 10^{-5}$ with an observed range of spectral index: $0.92 \leq n_s \leq 1.0$ (within 2σ error bar) [2]. The inflaton carries SM gauge charges, and hence naturally produces (a thermal bath of) the SM degrees of freedom [3, 4]. If the reheat temperature of the universe is higher than the mass of the inflaton, then the plasma upon reheating will, in addition, have a thermal distribution of the inflaton quanta. If the inflaton is absolutely stable, due to some symmetry, then it can also serve as the cold dark matter. Once the temperature drops below the inflaton mass, its quanta undergo thermal freeze-out and may yield the correct dark matter abundance. As a consequence, direct and indirect dark matter detection experiments will provide valuable information about the inflaton couplings to the SM fields.

The main question is whether relic density of the inflaton after thermal freeze-out can account for dark matter in the universe. For particles with gauge interactions, the unitarity bound puts an absolute upper bound ~ 100 TeV on their mass [5]. For smaller couplings this bound will decrease in order to have acceptable thermal dark matter, for a review see [6]. Therefore, the inflaton mass should be below 100 TeV, which puts a severe constraint on the flatness of the inflaton potential. As we will show an inflaton with a weak scale mass and a tiny self-coupling can drive a successful inflation. Coincidentally such a small coupling is welcoming if the neutrinos are Dirac in nature [7]. It turns out that if the inflaton

is composed of the SM Higgs, slepton and the sneutrino, then it serves all three purposes: inflation, cold dark matter, and neutrino mass.

Let us consider the minimal supersymmetric standard model (MSSM) with three right-handed (RH) neutrino multiplets. We assume the neutrinos to be of Dirac type. Whether the nature of neutrino is Dirac or Majorana can be determined in the future neutrinoless double beta decay experiment. Then relevant superpotential term is

$$W \supset h \mathbf{N} \mathbf{H}_u \mathbf{L}. \quad (1)$$

Here \mathbf{N} , \mathbf{L} and \mathbf{H}_u are superfields containing the RH neutrinos, left-handed (LH) leptons and the Higgs which gives mass to the up-type quarks, respectively. For conciseness we have omitted the generation indices, and we work in a basis where neutrino Yukawa couplings h (and hence neutrino masses) are diagonalized.

For various reasons, which will become clear, the inclusion of a gauge symmetry under which the RH (s)neutrinos are not singlet is crucial. As far as inflation is concerned, a singlet RH sneutrino would not form a gauge-invariant inflaton along with the Higgs and slepton fields. We consider a minimal extension of the SM gauge group which includes a $U(1)$: $SU(3)_c \times SU(2)_L \times U(1)_Y \times U(1)_{B-L}$, where B and L denote the baryon and lepton numbers respectively. This is the simplest extension of the SM symmetry which is also well motivated: anomaly cancelation requires that three RH neutrinos exist, so that they pair with LH neutrinos to form three Dirac fermions.

In this model we have an extra Z boson (Z') and one extra gaugino (\tilde{Z}'). The $U(1)_{B-L}$ gets broken around TeV by new Higgs fields with $B-L = \pm 1$. This also prohibits a Majorana mass for the RH neutrinos at the renormalizable level (note that $\mathbf{N}\mathbf{N}$ has $B-L = 2$). The Majorana mass can be induced by a non-renormalizable operator, but it will be very small.

The value of h needs to be small, i.e. $h \lesssim 10^{-12}$, in order to explain the light neutrino mass, $\sim \mathcal{O}(0.1 \text{ eV})$ corresponding to the atmospheric neutrino oscillations

detected by Super-Kamiokande experiment ¹.

Note that the $\mathbf{NH}_u\mathbf{L}$ monomial represents a D -flat direction under the $U(1)_{B-L}$, as well as the SM gauge group [9]. (a flat direction represented by a polynomial is more involved [10]). The flat direction field ϕ is defined as

$$\phi = \frac{\tilde{N} + H_u + \tilde{L}}{\sqrt{3}}, \quad (2)$$

where \tilde{N} , \tilde{L} , H_u are the scalar components of corresponding superfields. Since the RH sneutrino \tilde{N} is a singlet under the SM gauge group, its mass receives the smallest contribution from quantum corrections due to SM gauge interactions, and hence it can be set to be the lightest supersymmetric particle (LSP). Therefore the dark matter candidate arises from the RH sneutrino component of the inflaton, see Eq. (2). The potential along the flat direction, after the minimization along the angular direction, is found to be [4],

$$V(|\phi|) = \frac{m_\phi^2}{2}|\phi|^2 + \frac{h^2}{12}|\phi|^4 - \frac{Ah}{6\sqrt{3}}|\phi|^3. \quad (3)$$

The importance of A -term in providing large vacuum energy was shown before [11]. The flat direction mass m_ϕ is given in terms of \tilde{N} , H_u , \tilde{L} masses:

$$m_\phi^2 = \frac{m_{\tilde{N}}^2 + m_{H_u}^2 + m_{\tilde{L}}^2}{3}. \quad (4)$$

Note that for $A = 4m_\phi$, there exists a *saddle point* for which $V'(\phi_0) = V''(\phi_0) = 0$. The saddle point and the potential are given by:

$$\phi_0 = \sqrt{3} \frac{m_\phi}{h} = 6 \times 10^{12} m_\phi \left(\frac{0.05 \text{ eV}}{m_\nu} \right), \quad (5)$$

$$V(\phi_0) = \frac{m_\phi^4}{4h^2} = 3 \times 10^{24} m_\phi^4 \left(\frac{0.05 \text{ eV}}{m_\nu} \right)^2. \quad (6)$$

Here m_ν denotes the neutrino mass which is given by $m_\nu = h\langle H_u \rangle$, with $\langle H_u \rangle \simeq 174 \text{ GeV}$. For neutrino masses with a hierarchical pattern, the largest neutrino mass is $m_\nu \simeq 0.05 \text{ eV}$ in order to explain the atmospheric neutrino oscillations [12], while the current upper bound on the sum of the neutrino masses from cosmology, using WMAP and SDSS data alone, is 0.94 eV [13].

Inflation can take place along the *gauge invariant* flat direction ϕ , near a saddle point ϕ_0 ². The dynamics of

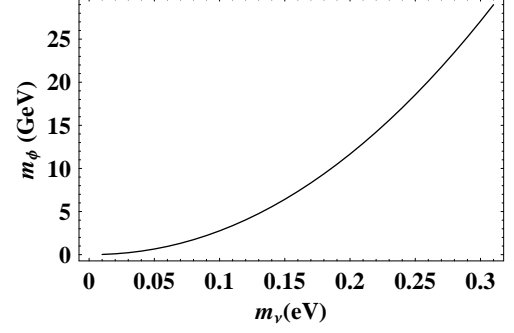


FIG. 1: The inflaton mass m_ϕ is plotted as a function of the neutrino mass m_ν .

the inflaton can be understood by expanding the potential, $V(\phi) = V(\phi_0) + (1/3!)V'''(\phi_0)(\phi - \phi_0)^3 + \dots$, see Refs. [3, 4]. The slow roll inflation is governed by the third derivative of the potential, $V'''(\phi_0) = (2/\sqrt{3})hm_\phi$. A sufficient number of e-foldings is generated during the slow roll, i.e. $\mathcal{N}_e \sim (\phi_0^2/m_\phi M_P)^{1/2}$ [4]. For $m_\phi \sim 50 \text{ GeV}$, it turns out to be $\mathcal{N}_e \sim 10^3$.

The amplitude of density perturbations follows [4].

$$\delta_H \simeq \frac{1}{5\pi} \frac{H_{inf}^2}{\dot{\phi}} \simeq 3.5 \times 10^{-27} \left(\frac{m_\nu}{0.05 \text{ eV}} \right)^2 \left(\frac{M_P}{m_\phi} \right) \mathcal{N}_{\text{COBE}}^2. \quad (7)$$

Here m_ϕ denotes the loop-corrected value of the inflaton mass at the scale ϕ_0 in Eqs. (5,6,7) ³. In Figure 1, we show the neutrino mass as a function of the inflaton mass. We use $\delta_H = 1.91 \times 10^{-5}$ to draw the plot. We see that the neutrino mass in the range 0 to 0.30 eV corresponds to the inflaton mass of 0 to 30 GeV. We will be using this mass range of the inflaton to calculate the SUSY masses which allow a RH sneutrino dark matter.

The spectral index of the power spectrum is given by $n_s = 1 + 2\eta - 6\epsilon \simeq 1 - 4/\mathcal{N}_{\text{COBE}}$, and the running in the spectral tilt is $dn_s/d\ln k = -4/\mathcal{N}_{\text{COBE}}^2$ [4]. Here $\mathcal{N}_{\text{COBE}}$ is the number of e-foldings between the time the observationally relevant perturbations were generated and the end of inflation. The exact number depends on the scale of inflation and on when the Universe becomes radiation dominated. As we shall see that the universe becomes radiation dominated instantly (time scale comparable to the Hubble scale) after the end of inflation. The required number of e-foldings is rather small, i.e. $\mathcal{N}_{\text{COBE}} \sim 40$ [15]. For such a low $\mathcal{N}_{\text{COBE}}$ the value of $n_s \sim 0.90$ near the saddle point. At a face value this is already ruled out by the WMAP data [2]. However a slight departure from a saddle point can provide the spectrum which is well inside the observed limit. In fact the spectral tilt can be obtained within $0.90 \leq n_s \leq 1.0$ if ϕ_0 be-

¹ One can assume that the neutrino mass terms are part of the Kähler potential Ref. [8]. One can then generate a small neutrino mass in the superpotential by Kähler transformation (similar to generation of μ parameter).

² This requires that the inflaton starts in the vicinity of ϕ_0 with $\dot{\phi}_0 \approx 0$ [14]. Around a saddle point there exists a self-reproduction regime such that most parts of the universe inflate forever [4].

³ Even though the inflaton potential gets loop corrections due to gauge interactions, the existence of a saddle point remains and the flatness of the potential is not ruined [4].

comes a point of inflection, i.e. $V'(\phi_0) \neq 0$, $V''(\phi_0) = 0$ [16, 17]. Note that its reflection on the amplitude of the density perturbations is negligible.

The inflaton has gauge couplings to the electroweak and $U(1)_{B-L}$ gauge/gaugino fields. It therefore induces a VEV-dependent mass $\sim g\langle\phi\rangle$ for these fields (g denotes a typical gauge coupling). After the end of inflation, ϕ starts oscillating around the global minimum at the origin with a frequency $m_\phi \sim 10^3 H_{\text{inf}}$. When the inflaton passes through the minimum, $\langle\phi\rangle = 0$, the induced mass undergoes non-adiabatic time variation. This results in non-perturbative particle production [18]. As the inflaton VEV is rolling back to its maximum value ϕ_0 , the mass of the gauge/gaugino quanta increases again. Because of their large couplings they quickly decay to the fields which are not coupled to the inflaton, hence massless, notably the down-type (s)quarks. This is a very efficient process as a result of which relativistic particles are created within few Hubble times after the end of inflation (for more details, see [17]). A thermal bath of MSSM particles is eventually formed with a temperature $T_R \sim 10^6$ GeV (for details of thermalization in SUSY, see [19]). Note that the reheat temperature is high enough for the electroweak baryogenesis [20]. On the other hand, it is sufficiently low to avoid overproduction of dangerous relics such as gravitinos [19, 21].

Scatterings via the new $U(1)$ gauge interactions also bring the RH sneutrino into thermal equilibrium. Note that part of the inflaton, i.e. its \tilde{N} component see Eq. (2), has never decayed; only the coherence in the original condensate that drives inflation is lost. Its relic abundance will be then set by thermal freeze-out. The fact that \tilde{N} has gauge interactions under the new $U(1)$ is crucial in this respect: the neutrino Yukawa h is way too small to allow acceptable thermal dark matter ⁴.

Note that the mass of dark matter (i.e. RH sneutrino) is correlated with the inflaton mass, see Eq. (4). However, the former is calculated at the weak scale, while the latter is at the scale ϕ_0 , see Eq. (5). The two quantities are related to each other by RGEs. In order to calculate the masses in the model, we use SUGRA boundary conditions (i.e. m_0 : universal scalar mass for the squarks and sleptons (but the Higgs masses are different), $m_{1/2}$: universal gaugino mass, A_0 : trilinear scalar coupling, $\mu > 0$ and $\tan\beta$) for the sparticle masses in the extended $U(1)$ model. We also assume that the gauge couplings are unified at the GUT scale. Then the new gauge coupling is of the order of hypercharge gauge coupling.

Even though the inflaton mass is small at the scale ϕ_0 , obtained by solving Eq. (5), the RGE effects increase the RH sneutrino and slepton masses at the weak scale. Note

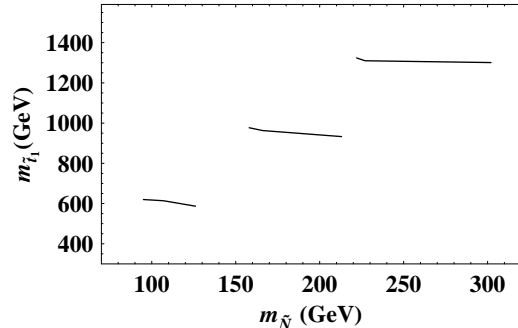


FIG. 2: $m_{\tilde{\nu}_1}$ vs $m_{\tilde{N}}$. The lines are for neutrino masses 0.3 eV. The gluino masses for the three lines are 730, 1200 and 1640 GeV (bottom-up). For smaller neutrino masses, the lines are slightly shifted downwards.

that $m_{\tilde{N}}$ and $m_{\tilde{L}}$ are soft breaking masses, while m_{H_u} also includes the contribution from the μ term. In Figure 2 we plot the RH sneutrino and stop masses at the weak scale for different values of gluino masses. The gluino masses for the three lines (solid and dashed) are 730 GeV, 1.20 TeV and 1.64 TeV (bottom-up). The lines are drawn for 0.30 eV neutrino mass. If we choose the neutrino masses to be 0.05 eV, the lines do not shift much. The left and right end of the lines correspond to $m_0=0$ and $m_{\tilde{\nu}} > m_{\tilde{\chi}^0}$. The charged sleptons and the LH sneutrinos are more massive compared to the RH sneutrino since these particles get contributions from more gaugino loops due to their $SU(2)_L$ and $U(1)_Y$ couplings. Figure 2 shows that the masses of sparticles (e.g., the lighter stop) can be within the reach of initial phase of the LHC.

In order to calculate the relic abundance of the RH sneutrino, we need to know the masses of the additional gauge boson Z' and its SUSY partner \tilde{Z}' , the new Higgsino masses, Higgs VEVs which break the new $U(1)$ gauge symmetry, the RH sneutrino mass, the new gauge coupling, and the charge assignments for the additional $U(1)$. We assume that the new gauge symmetry is broken around 2 TeV ⁵, and the existence of two new Higgs superfields to maintain the theory anomaly free. The primary diagrams responsible to provide the right amount of relic density are mediated by \tilde{Z}' in the t -channel. In Figure 3, we show the relic density values for smaller masses of sneutrino where the lighter stop mass is $\lesssim 1$ TeV. The smaller stop mass will be easily accessible at the LHC and is also preferred by the little hierarchy solutions [22]. We have varied new gaugino and Higgsino masses and the ratio of the VEVs of new Higgs fields to generate Fig. 3. We find that the WMAP [2] allowed values of the relic density, i.e., 0.094 – 0.129 is satisfied for many points. In the case of a larger sneutrino mass

⁴ Or acceptable sneutrino dark matter at all. Note that \tilde{N} would dominate the universe right after the end of inflation if it had no gauge interactions. h is too small to deplete the energy in the \tilde{N} component of the inflaton via non-perturbative particle production.

⁵ This is sufficient to ensure that the RH neutrinos decouple from the thermal bath early enough in order not to affect big bang nucleosynthesis (BBN).

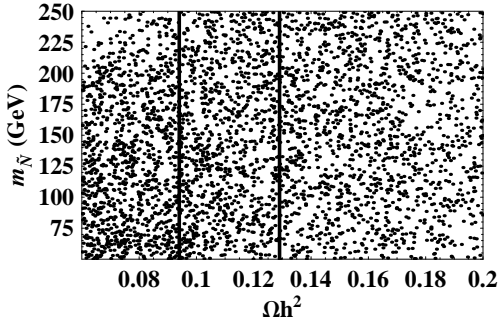


FIG. 3: Ωh^2 vs $m_{\tilde{N}}$. The solid lines from left to right are for $\Omega h^2 = 0.094$ and 0.129 respectively. The Z' -ino mass is equal to the Bino mass since the new $U(1)$ gauge coupling is the same as the hypercharge gauge coupling.

in this model, the correct dark matter abundance can be obtained by annihilation via Z' pole [23].

Since the dark matter candidate, the RH sneutrino, interacts with quarks via the Z' boson, it is possible to see it via the direct detection experiments. The detection cross sections are not small as the interaction diagram involves Z' in the t -channel. The typical cross section is about 2×10^{-8} pb for a Z' mass around 2 TeV. It is possible to probe this model in the upcoming dark matter

detection experiments [24]. The signal for this new scenario at the LHC will contain standard jets plus missing energy and jets plus leptons plus missing energy. The jets and the leptons will be produced from the cascade decays of squarks and gluinos into the final state containing the sneutrino.

In conclusion, within a minimal extension of the SM, we can explain our universe with observed temperature anisotropy in the CMB, the right abundance of thermal dark matter, and the Dirac neutrino masses. More importantly, this is a scenario which we can test in laboratory. The dark matter candidate, which is part of the inflaton, is detectable in direct detection experiments and in the colliders. Thus it provides us hints on the inflaton, which is believed to be the most elusive particle in the universe. The future neutrinoless double beta decay experiments will lead to valuable information on the nature of neutrinos and this scenario.

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